

Name \_\_\_\_\_ Per \_\_\_\_\_

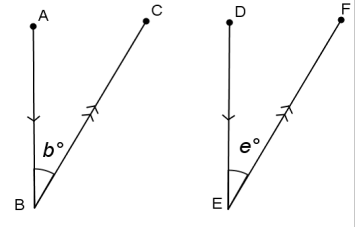
LO: I can add auxiliary lines to diagrams and use angle relationships to prove statements.

DO NOW On the back of this packet

(1) **Angles: Exterior angle theorem:** Proof by constructing a parallel line.

transparencies, dry erase markers, erasers compass

Using the diagram at right, Tyasia and Taleak are proving that the measures of angles B and E are equal. Why do they need to extend lines or add auxiliary lines?




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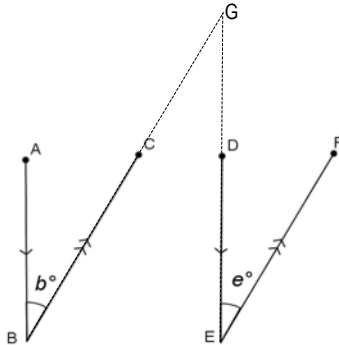


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Tyasia's diagram



Describe Tyasia's additions to the diagram

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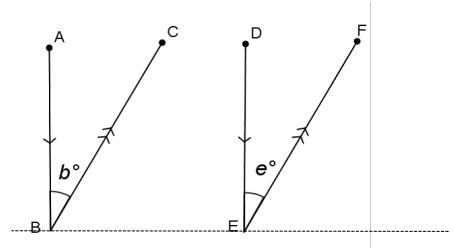


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Taleak's diagram



Describe Taleak's additions to the diagram

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Tyasia says she can use alternate interior angles to write her proof. Do you agree with her? Why or why not?

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Taleak says he can use corresponding angles to write his proof. Do you agree with him? Why or why not?

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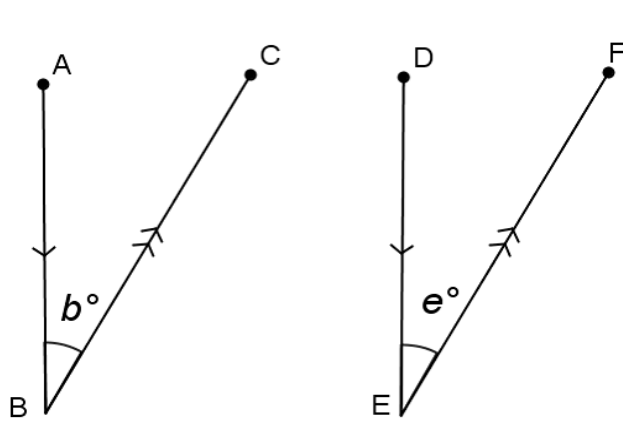
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(1)

**Angles: Proving relationships**

cont.  
transparenc  
ies, dry  
erase  
markers,  
erasers

Choose ONE of their drawings and prove that the measure of angle B is equal to the measure of angle E. Add letters to the diagram where needed to help you write the proof



I know that ...

because ...


(2) transparencies, dry erase markers, erasers

**Angles: Proving relationships**

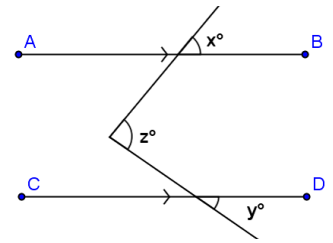
The diagrams that Tyasia and Taleak drew could BOTH be used to write the proof.

Like problem #1, there is more than one way to add to the diagram at right

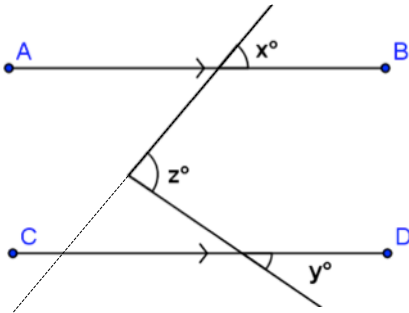
to prove the statement below.

Given:  $\overline{AB} \parallel \overline{CD}$

Prove:  $z = x + y$



The three diagrams below have different extensions or auxiliary lines drawn. Add the letters *a* and *b* to each diagram to help you write the proof.

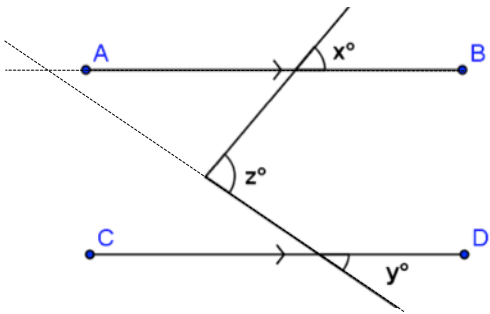


**THINK:** Angle *z* is an interior/exterior (circle one) angle of the triangle formed.

An \_\_\_\_\_ angle of a triangle is equal to the sum of the \_\_\_\_\_ angles. If we can get the remote interior angles to be the same measures as \_\_\_\_\_ and \_\_\_\_\_, then we can prove that  $z = x + y$

**PROOF:**

- (1)  $a = x$  because the angles are corresponding (add *a* to the diagram)
- (2)  $b = y$  because they are vertical (add *b* to the diagram)
- (3) \_\_\_\_\_ + \_\_\_\_\_ =  $z$  because of the \_\_\_\_\_ thm.
- (4) \_\_\_\_\_ + \_\_\_\_\_ =  $z$  because equal values can be substituted.

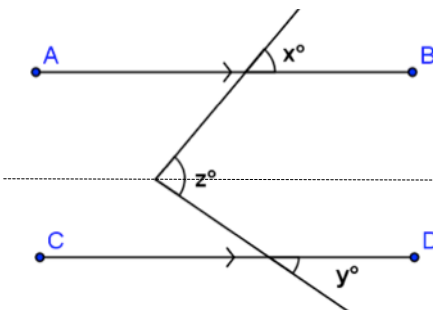


**THINK:** Angle *z* is an interior/exterior (circle one) angle of the triangle formed.

An \_\_\_\_\_ angle of a triangle is equal to the sum of the \_\_\_\_\_ angles. If we can get the remote interior angles to be the same measures as \_\_\_\_\_ and \_\_\_\_\_, then we can prove that  $z = x + y$

**PROOF:**

- (1)  $a = x$  because the angles are \_\_\_\_\_ (add *a* to the diagram)
- (2)  $b = y$  because they \_\_\_\_\_ (add *b* to the diagram)
- (3) \_\_\_\_\_ + \_\_\_\_\_ =  $z$  because of the \_\_\_\_\_ theorem.
- (4) \_\_\_\_\_ + \_\_\_\_\_ =  $z$  because equal values can be \_\_\_\_\_.



**THINK:** Angle *z* is composed of \_\_\_\_\_ adjacent angles. If we can prove that one of the angles is congruent to \_\_\_\_\_ and the other is congruent to \_\_\_\_\_ then we can prove that  $z = x + y$

**PROOF:**

- (1)  $a = x$  because the angles are \_\_\_\_\_ (add *a* to the diagram)
- (2)  $b = y$  because the angles are \_\_\_\_\_ (add *b* to the diagram)
- (3) \_\_\_\_\_ + \_\_\_\_\_ =  $z$  because the measure of an angle is equal to the sum of the \_\_\_\_\_ angles that make up the larger angle.
- (4) \_\_\_\_\_ + \_\_\_\_\_ =  $z$  because \_\_\_\_\_.

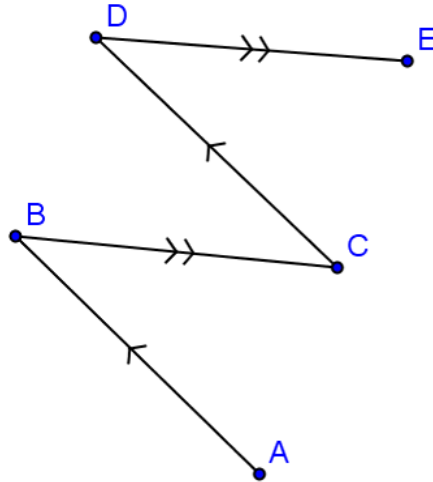
(3)  
large dry  
erase  
problems

### Angles: Proving Relationships

Prove the statement for each problem in this section. You may or may not need to draw an auxiliary line.

(a) In the figure,  $AB \parallel CD$  and  $BC \parallel DE$ .

Prove that  $\angle ABC = \angle CDE$ .



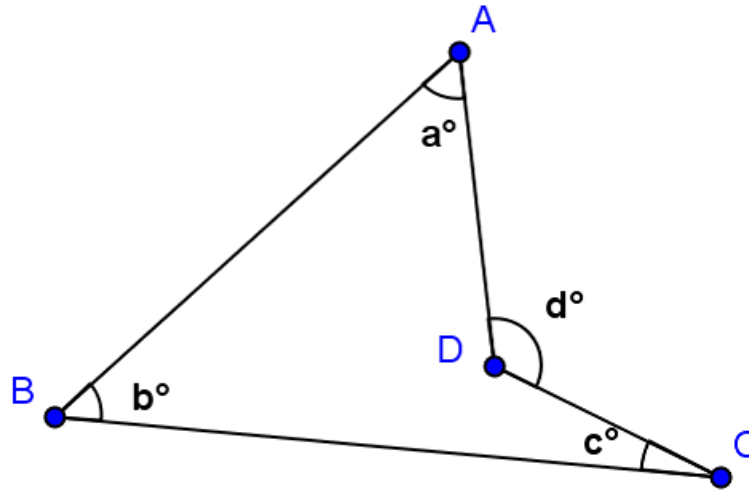
I know that ...

because ...


(3)  
large dry  
erase  
problems

**Angles: Proving Relationships**

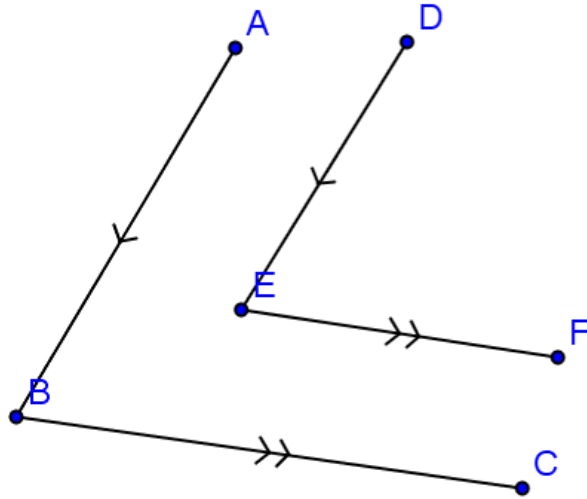
(b) In the figure, prove that  $d = a + b + c$ .



I know that ...	because ...

(3) **Angles: Proving Relationships**

cont.

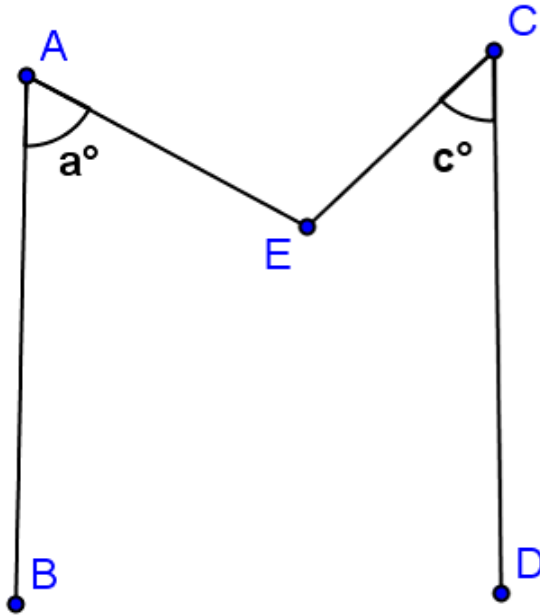
 (c) In the figure,  $AB \parallel DE$  and  $BC \parallel EF$ . Prove that  $\angle ABC = \angle DEF$ .

I know that ...	because ...

(3) **Angles: Proving Relationships**

cont.

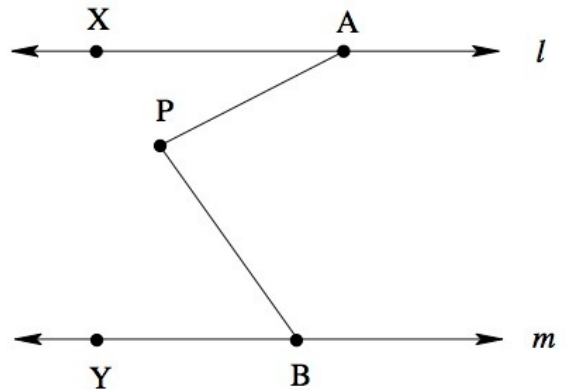
(d) In the figure,  $AB \parallel CD$ . Prove that  $\angle AEC = a + c$



I know that ...	because ...

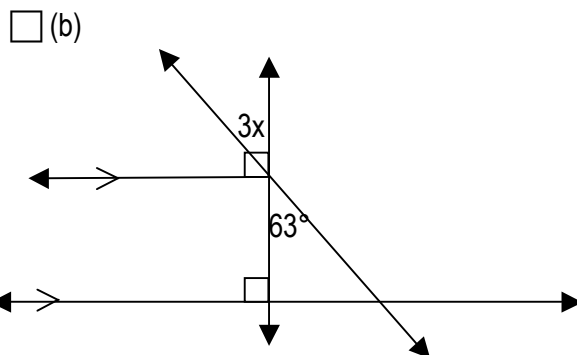
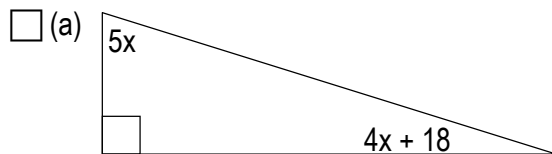
(4) **Exit Ticket**

ON THE LAST PAGE

 (5) **Homework**
 (1) PROVE:  $\angle XAP + \angle YBP = \angle APB$ 


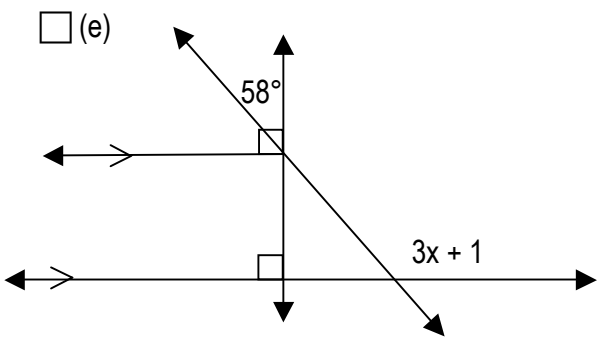
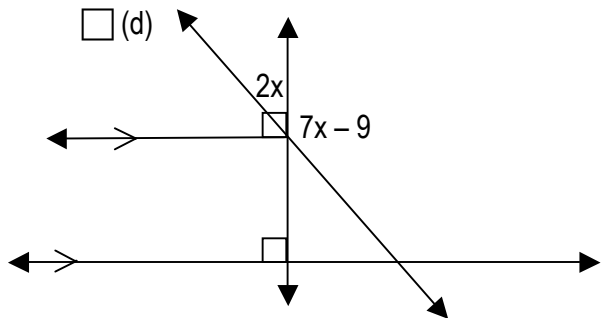
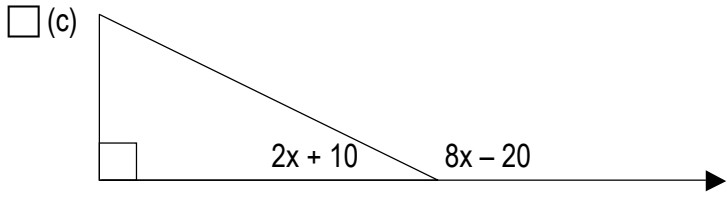
I know that ...

because ...


 (2) Find the measure of  $x$  in each diagram. State a reason for each step that you take.




(5) Homework  
cont.

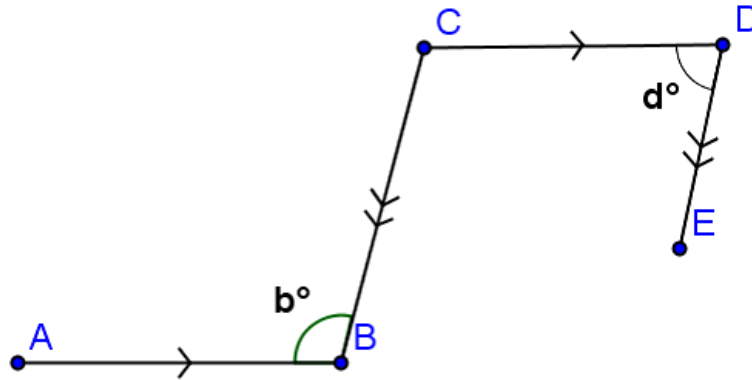




Exit Ticket Name \_\_\_\_\_ Date \_\_\_\_\_ Per \_\_\_\_\_ 3.6R

(1) The LO (Learning Outcomes) are written below your name on the front of this packet. Demonstrate your achievement of these outcomes by doing the following:

In the figure,  $AB \parallel CD$  and  $BC \parallel DE$ . Prove that  $b + d = 180$ .

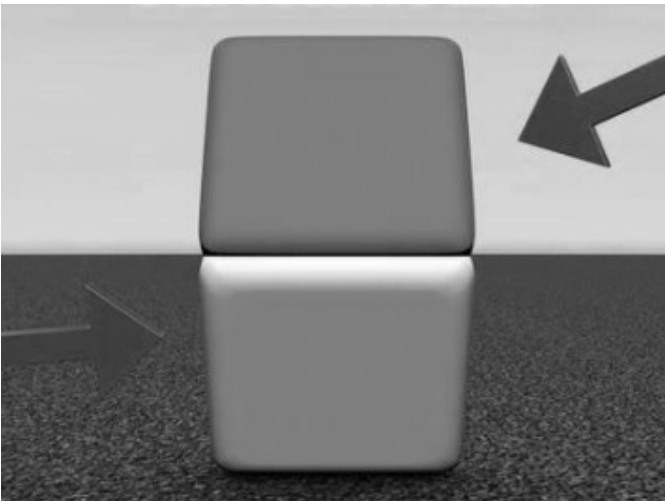


**DO NOW** Name \_\_\_\_\_ Date \_\_\_\_\_ Per \_\_\_\_\_

**3.6R**

- (1) Make 3 sketches: one that shows corresponding angles, one that shows alternate interior angles, and one that shows alternate exterior angles.

- (2) Are the boxes below the same color? \_\_\_\_\_ Now put your finger across the middle. Did this change your answer?



What a difference a line can make.